

Overview of LDX Results

Jay Kesner, A. Boxer, J. Ellsworth, I. Karim **Columbia University**

MIT

D.T. Garnier, A. Hansen, M.E. Mael, E.E. Ortiz

Columbia University

Paper VP1.00020

Presented at the APS Meeting, Philadelphia, November 2, 2006



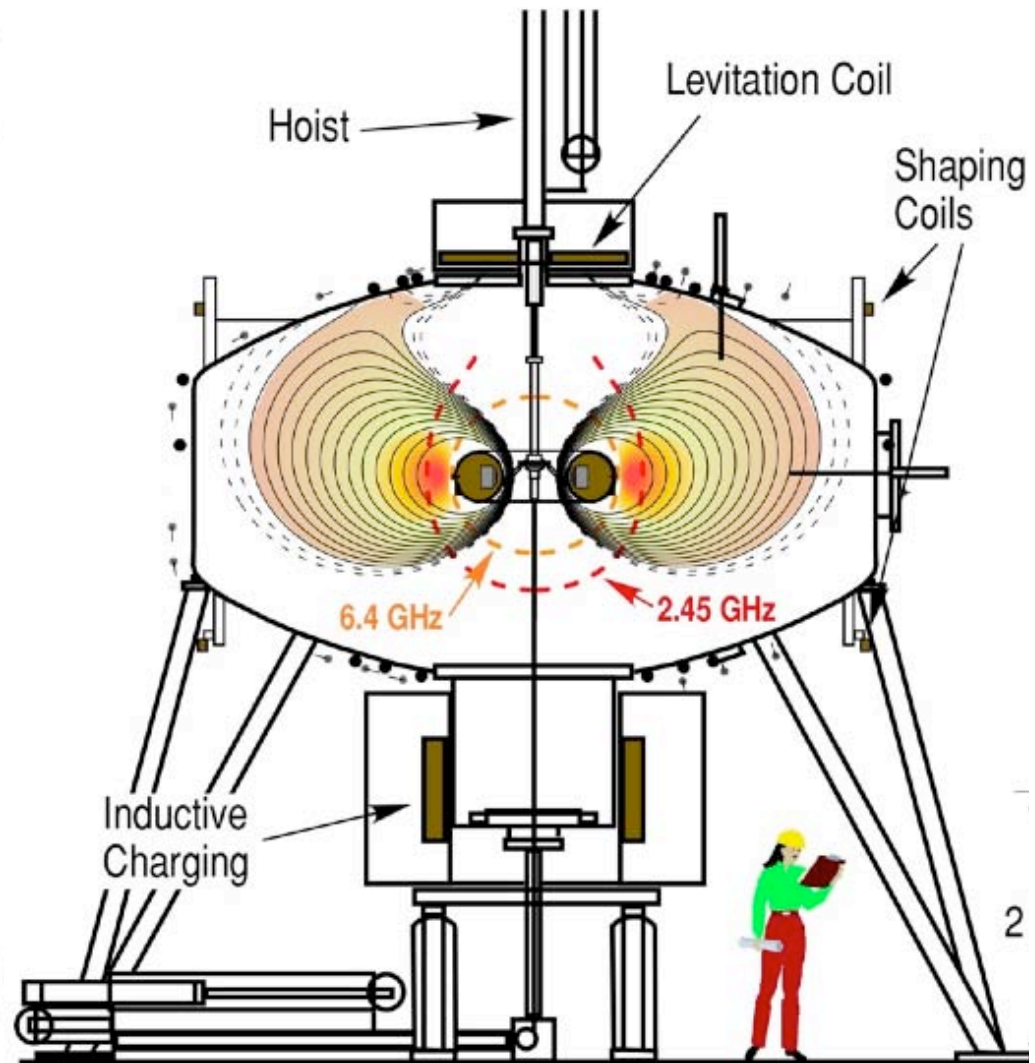
Outline of Poster

- Introduction to LDX
- MHD Equilibrium: High β results with ECRH
 - $\beta_{\max} \sim 20\%$ with $P_{\text{ECRH}} \sim 5 \text{ KW}$, $p_{\perp}/p_{\parallel} \approx 5$
- Hot electron interchange instability observed
 - Controlled by gas puffing affecting n_{eh}/n_i
- Low frequency drift modes
 - Controlled by gas puffing effecting $\text{grad}(n_{\text{eb}})$
- Power source implications
 - Ideal for advanced fuel DD reactor
- Future plans and conclusions

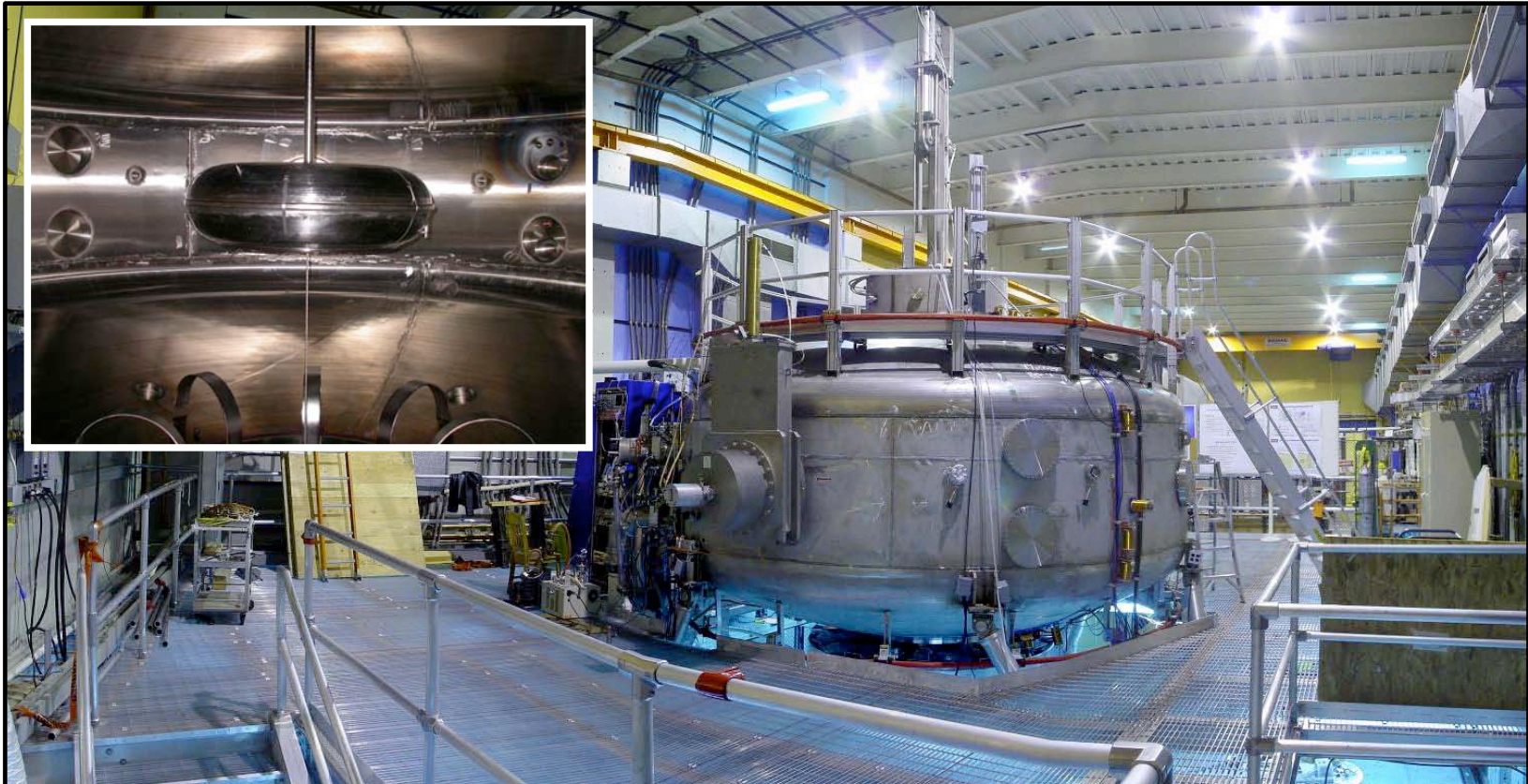
LDX Cross-Section/Operation

Supported Mode

- 1) Liquid Helium cools F-coil in charging station
- 2) Inductively charge F-coil (1 MA), C-coil discharges
- 3) Lift F-coil into position
- 4) Use ECRH (5 kW); create plasma
- 5) Run experiments safely for two hours
- 6) Lower F-coil back to re-charge or discharge into charging station



The Levitated Dipole Experiment (LDX)

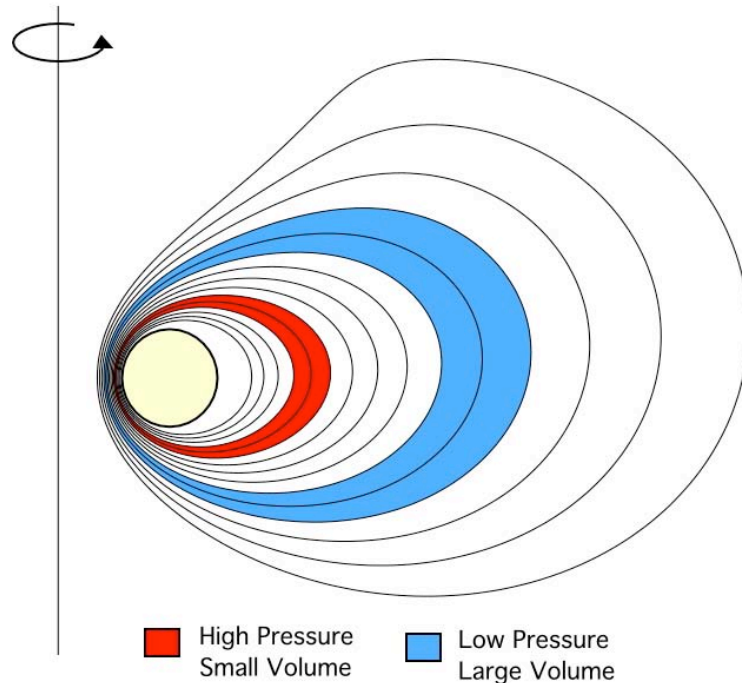


LDX utilizes 3 operating superconducting magnets

- Floating coil: (shown) Nb^3Sn (1.5 MA)
- Charging coil: NbTi (12 MJ, $B_{\text{max}}=5.6\text{T}$, 4.5K)
- Levitation coil: High T_c , BSSCO-2223 (20 kJ at 20K)

Ref: Garnier et al., to be published in Fusion Engineering and Design (2006).

Dipole Plasma Confinement



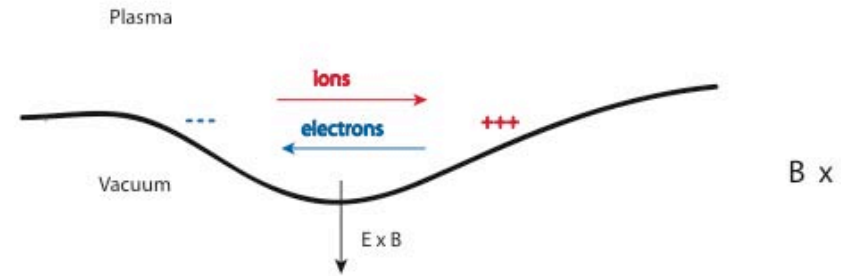
If $p_1 V_1^\gamma = p_2 V_2^\gamma$, then interchange does not change pressure profile.

For $\eta = \frac{d \ln T}{d \ln n} = \frac{2}{3}$, density and temperature profiles are also stationary.

- Toroidal confinement without toroidal field
 - Stabilized by plasma compressibility
 - Shear free
- Poloidal field provided by internal coil
 - Steady-state w/o current drive
 - $J_{||} = 0 \Rightarrow$ no kink instability drive
 - No neoclassical effects
 - No TF or interlocking coils
 - ∇p constraint \Rightarrow small plasma in large vacuum vessel
 - Convective flows transport particles w/o energy transport

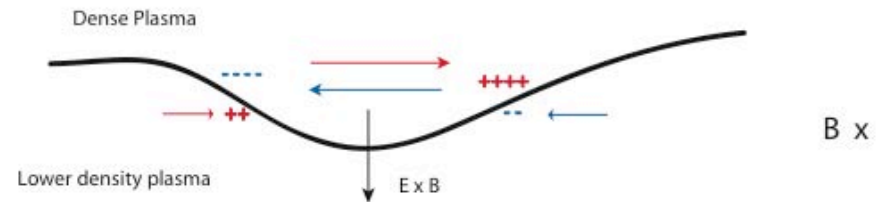
Dipole Stability Results from Compressibility

- No compressibility:
 “bad” κ & ∇B drifts causes charge separation \Rightarrow
 $V_{E \times B}$ increases perturbation



- With compressibility: as plasma moves downwards pressure decreases. For critical gradient there is no charge buildup

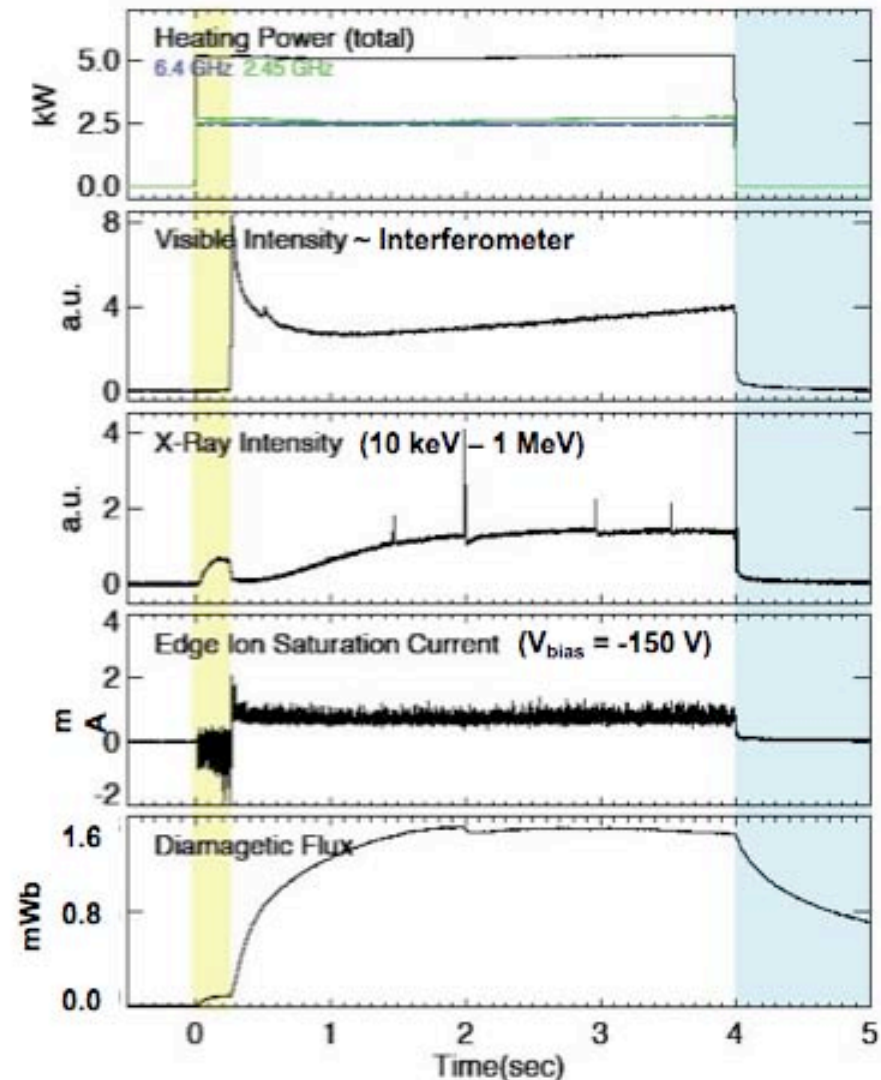
Density gradient.
 Compressibility: Density decreases as plasma moved downward.



In bad curvature pressure gradient is limited to $-\frac{d \ln p}{d \ln V} < \gamma$ $V = \oint dl / B$

Typical High Beta Discharge

- High beta maintained in quasi-steady state
- Plasma diagnostics:
 - External magnetic flux loops, pick-up coils and hall sensors
 - X-ray detectors
 - Visible diode array
 - Fixed & swept Langmuir
 - Interferometer
- HEI observed during three distinct intervals
 1. Unstable plasmas
 2. High beta plasmas
 3. Afterglow plasmas



Magnetic Equilibrium Reconstruction

- Equilibrium reconstruction demonstrate that plasmas with high local beta are created in LDX
- X-ray images show the fast electrons to be localized at the ECRH resonance. The fast electrons are anisotropic.
- Anisotropic equilibria are well fit to magnetic measurements. The equilibria have pressure gradients that exceed the usual MHD instability limits.
- New magnetic diagnostics will be installed closer to the plasma to distinguish more details of the pressure profile.

Magnetic Reconstruction

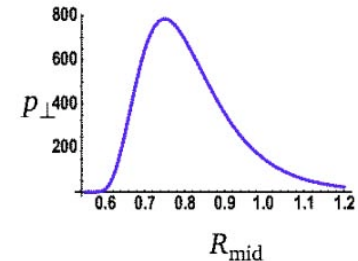
- Use pressure model from [Connor,Hastie, PF19,(1976)],

$$p_{\parallel}(\psi,B) = p_0(\psi)(B_0(\psi)/B)^2 p \quad \text{and} \quad p_{\perp}(\psi,B) = (1+2p) p_{\parallel}(\psi,B)$$

p is a constant $p=1/2$ ($p_{\perp}/p_{\parallel}-1$) and 0 subscript is for midplane.

- Parallel momentum balance gives $J_{\phi} = \frac{B \times \nabla p_{\perp}}{B^2} + (p_{\parallel} - p_{\perp}) \frac{B \times \kappa}{B^2}$
- Use 26 magnetic measurements to reconstruct profile

- Pressure model: $p_0(\psi) = p_{peak} \frac{(\psi - \psi_{fcoil})}{(\psi_{peak} - \psi_{fcoil})} (\psi / \psi_{peak})^{4g}$
optimize the fit varying p_{peak} , ψ_{peak} & g .



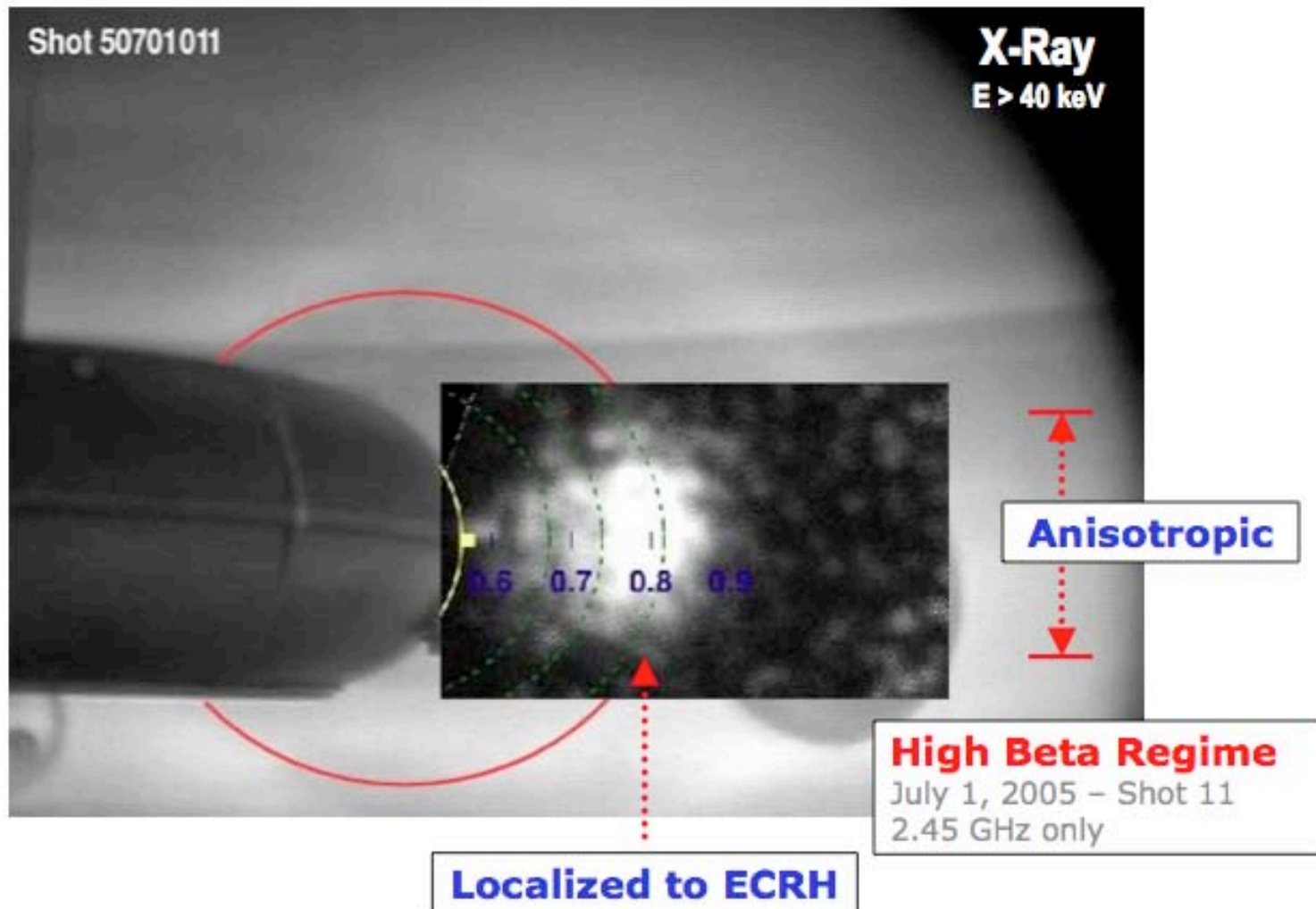
- We can obtain ψ_{peak} from X-ray measurements and find this yields best fits.

Anisotropic Interchange Stability

- Anisotropic momentum balance: $\frac{\partial p_{\parallel}}{\partial B} = \frac{p_{\parallel} - p_{\perp}}{B}$ $\frac{\partial p_{\perp}}{\partial B} = \frac{c + 2p_{\perp}}{B}$
- A convenient form for pressure is [Connor, Hastie, PF19, (1976)]:
 $p_{\parallel}(\psi, B) = p_0(\psi)(B_0(\psi)/B)^{2p}$ and $p_{\perp}(\psi, B) = (1 + 2p)p_{\parallel}(\psi, B)$
 $B_0(\psi)$ is the magnetic field on the outer midplane
- Defining $V_p = \oint dl / B^{(1+2p)}$ and $\hat{\gamma} = \frac{5}{3} \frac{1 + (4/5)p}{1 + (4/3)p}$ the interchange stability requirement becomes [Simakov, Hastie, Catto Ph.P 7 (2000)]

$$-\frac{d \ln p_0}{d\psi} < \hat{\gamma} \frac{d \ln V}{d\psi} + 2p \frac{d \ln B_0}{d\psi}$$
- For $p=0$ (isotropic pressure) obtain: $-\frac{d \ln p_0}{d\psi} < \gamma \frac{d \ln V_0}{d\psi}$ $V_0 = \oint dl / B$
- For $p \neq 0$ find requirement: $-\frac{d \ln p_0}{d\psi} < \hat{\gamma} \frac{d \ln V_p}{d\psi} + 2p \frac{d \ln B_0}{d\psi}$
 \therefore Evaluating RHS for $p=2$ critical gradient increases 3%. Anisotropy does not significantly change stability limit.

Anisotropic Fast Electrons Localized to ECRH Resonance



Anisotropy Significantly Changes Pressure Profile Height

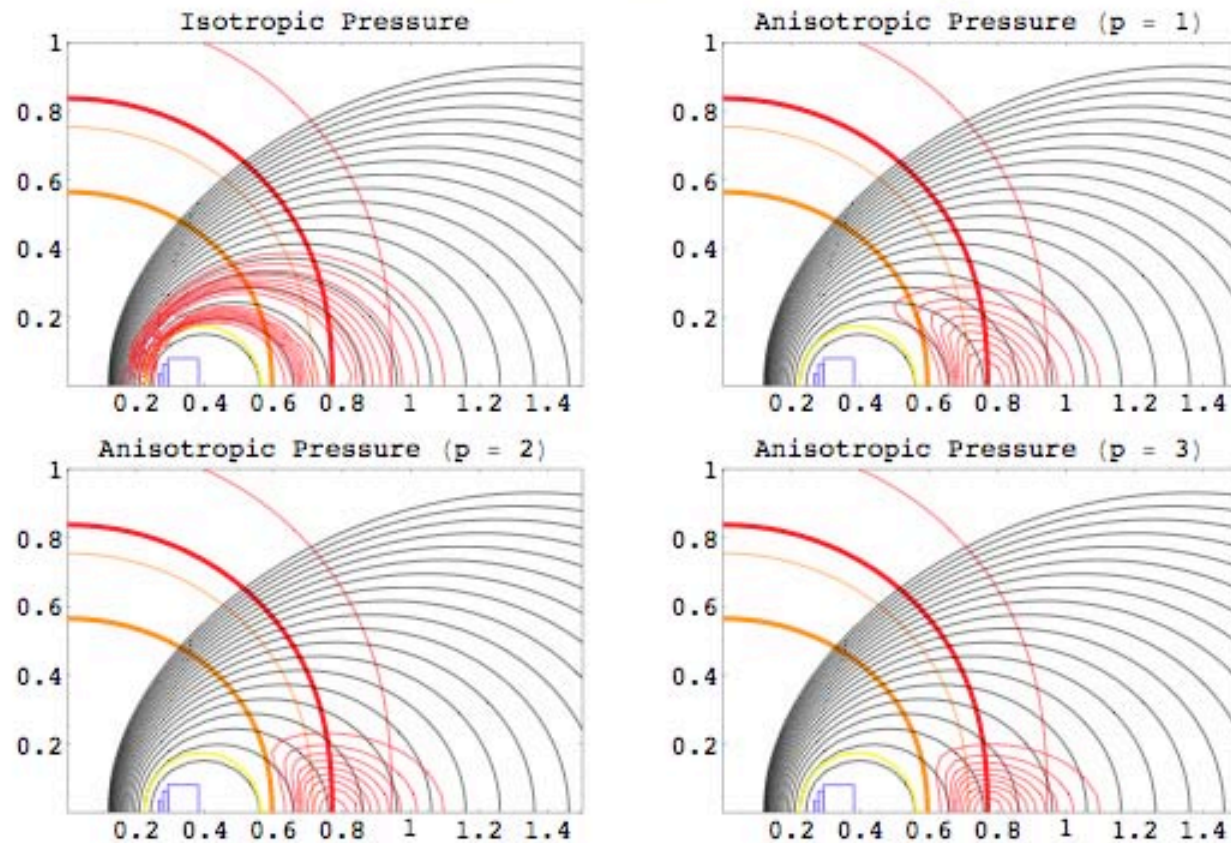
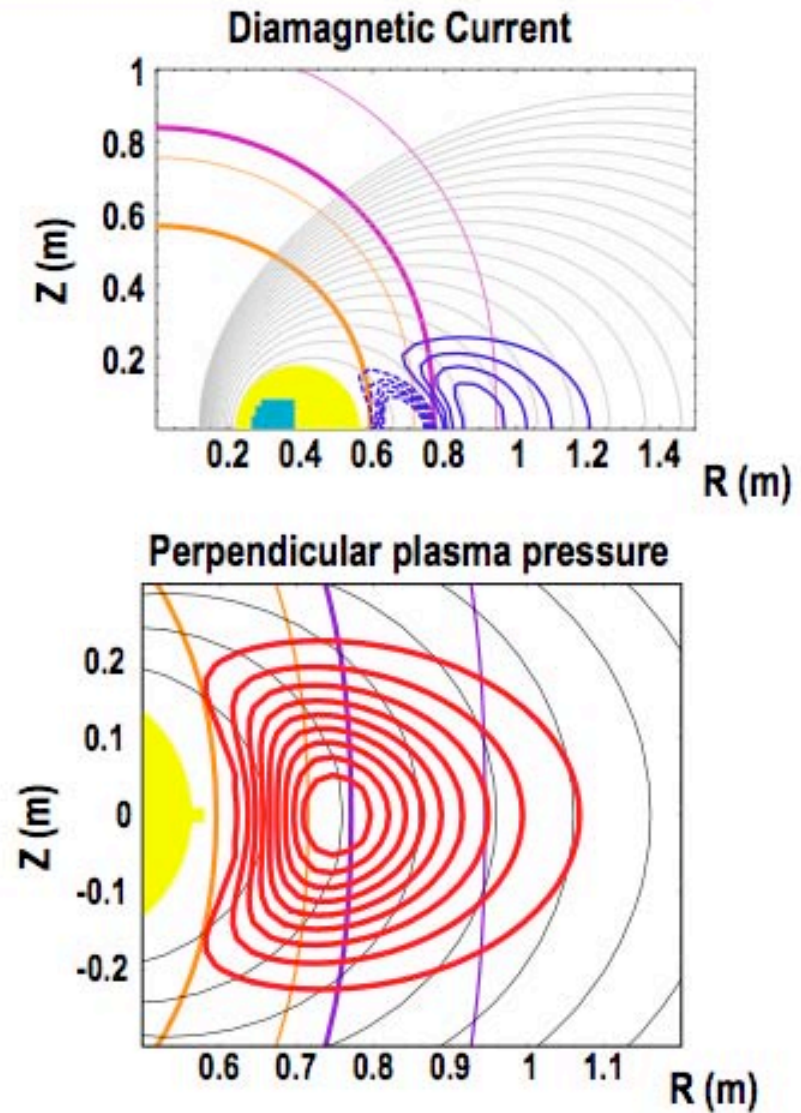


Figure 1: Example anisotropic pressure profiles with $G(\psi)$ defined with $g = 4$ and ψ_0 located at $r = 0.77$ m. The anisotropy parameter was $p = 0, 1, 2,$ and 3 .

Anisotropic Magnetics Reconstruction

- Shot 50513029
- Fixed from imaging
 - ▶ $R_{\text{peak}} = 0.75 \text{ m}$
 - ▶ $p_{\perp} / p_{\parallel} = 5$
- Magnetics fit
 - ▶ $E_{\text{total}} = 330 \text{ J}$ with 5 kW input
 - ▶ $I_p = 3.4 \text{ kA}$
 - ▶ $\beta_{\text{max}} \sim 20\%$
- $g = 2.1 * \gamma$,
 ∇p exceeds MHD



Hot Electron Interchange Stability

- Bulk plasma must satisfy MHD adiabaticity condition

Rosenbluth and Longmire, (1957)

$$\delta (p_b V^{\gamma}) = 0$$

where $V = \oint \frac{d\ell}{B}$ or $-\frac{d \ln p_b}{d \ln V} < \gamma^{-1}$

- Fast electron stability enhanced due to coupling of fast electrons to background ions

Krall, (1966)

$$-\frac{d \ln n_{eh}}{d \ln V} < 1 + \frac{m_{\perp}^2}{24} \frac{\omega_{dh}}{\omega_{ci}} \frac{N_i}{N_{eh}}$$

HEI Appear Under Three Conditions

See poster VP1.00024, Ortiz et al

- Continuous Bursts:
 - Unstable plasmas, low beta, low-density
- Minor Relaxation:
 - Short, low-amplitude, remains at high **beta**
- Total Energy Collapse:
 - Intense, large-amplitude, rapid density & fast electron beta loss

Physics of Hot Electron Interchange (HEI) Mode

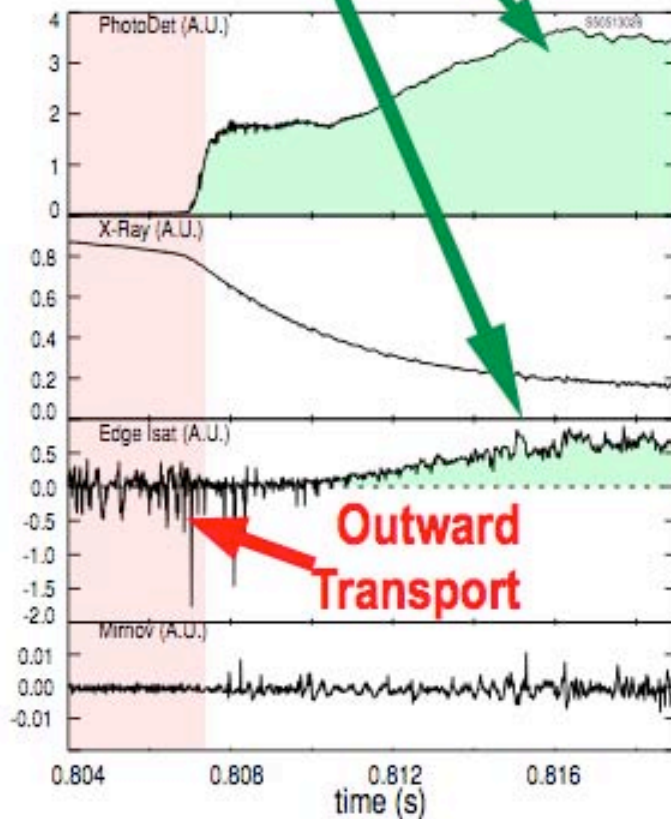
- Interchange instability driven by fast electrons
- HEI instability resonates with the drift motion of fast electrons. Causes a REAL frequency, $\omega \sim m \omega_d$
- Stable beyond the usual ideal MHD Limit
- As documented in low **beta** dipole experiment (CTX), HEI has the following characteristics:
 - Rapid outward transport with broad frequency spectrum
 - Dominated by low- m numbers
 - Broad global radial mode structure
 - Nonlinear frequency sweeping corresponds to radial propagation of “phase-space holes”

High **Beta** Control with Gas Puffing

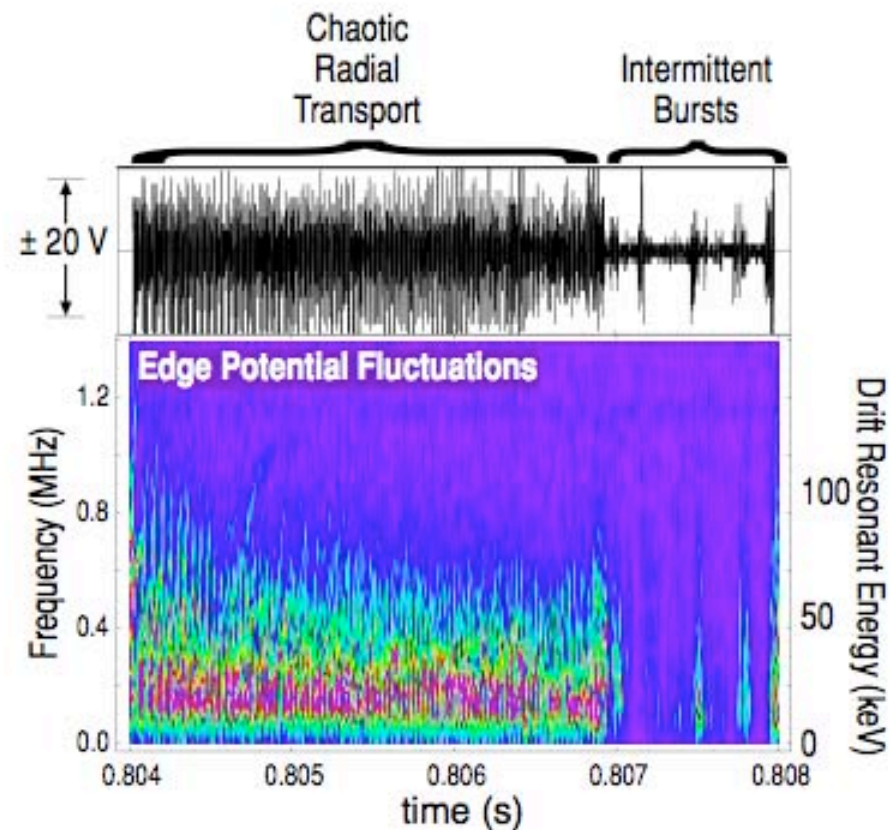
- With sufficient neutral gas pressure, plasma enters high **beta** regime
- With insufficient neutral gas pressure, the plasma will become unstable (sometimes violently)
- A hysteresis in the observed thresholds implies the bifurcation of the low density unstable and stable high **beta** regimes
- Consistent with theory of the Hot Electron Interchange (HEI) instability

High- β Plasma Begins Upon HEI Stabilization

Rapid Ionization and Density Rise = Stability



In unstable regime, quasi-continuous HEI instability prevents plasma build-up ...

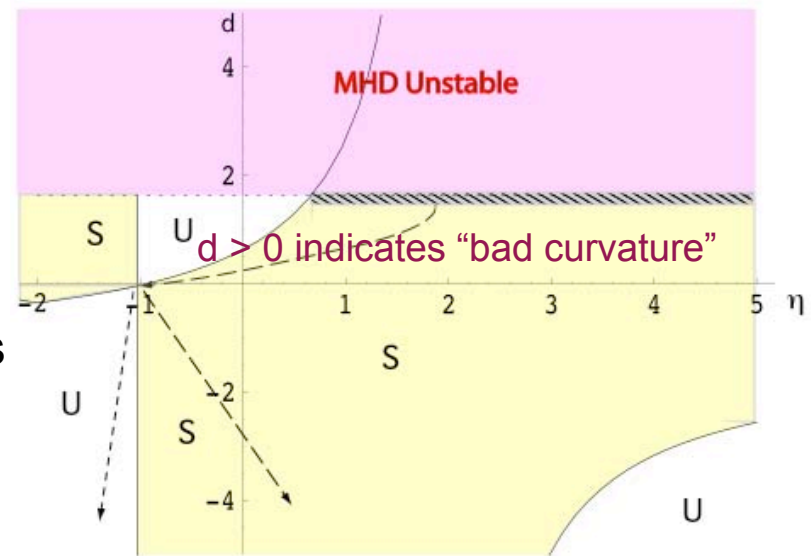


Plasma can be unstable to drift frequency mode

- Entropy mode properties [1]
 - Plasma beyond pressure peak stable for $\eta > 2/3$
 - Frequency $\omega \sim \omega_* \sim \omega_d$
 ω increases with ∇n_e and T_b
 - Instability will relax plasma towards $d=5/3, \eta=2/3$.

i.e. it tends to steepen ∇n_e

- Stability in good curvature region depends on sign of ∇n_e
- Mode appears at both high and low collisionality [2].
- Electrostatic “entropy” mode persists at high β [3].
- [Linear theory not always relevant to real plasmas](#)



$$\eta = d \ln T / d \ln n_e$$

$$d = -d \ln p / d \ln V = \omega_{*i} (1 + \eta) / \overline{\omega_d}$$

$$V = \oint dl / B$$

Some references:

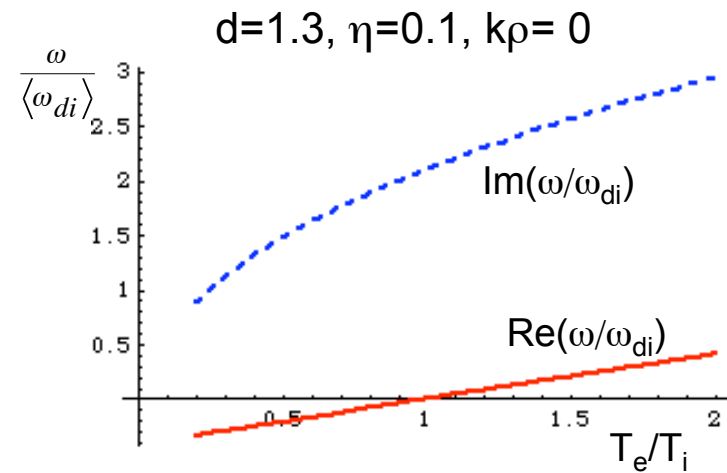
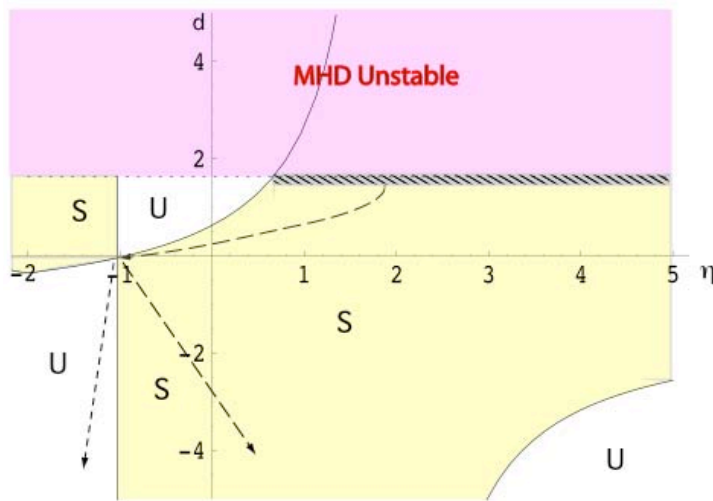
1. Kesner, PoP **7**, (2000) 3837.
2. Kesner, Hastie, Phys Plasma **9**, (2002), 4414
3. Simakov, Catto et al, PoP **9**, (2002), 201

Plasma can be unstable to drift frequency mode

- Entropy mode is a drift frequency, flute mode.

- Dispersion Relation $\hat{\omega} = \omega / \langle \omega_{di} \rangle$, $d = -\frac{d \ln p}{d \ln V} = (1 + \eta) \frac{\omega_{*i}}{\langle \omega_{di} \rangle}$, $\eta = \frac{d \ln T}{d \ln n}$

$$\hat{\omega}^2 \left(\frac{d \ln p}{d \ln V} + \frac{5}{3} \right) + \frac{5\hat{\omega}}{3} \left(\frac{T_e}{T_i} - 1 \right) \left(\frac{d \ln p / d \ln V}{1 + \eta} + 1 \right) + \frac{5}{9} \frac{T_e}{T_i} \left(\frac{d \ln p}{d \ln V} \frac{3\eta - 7}{\eta + 1} - 5 \right) = 0$$

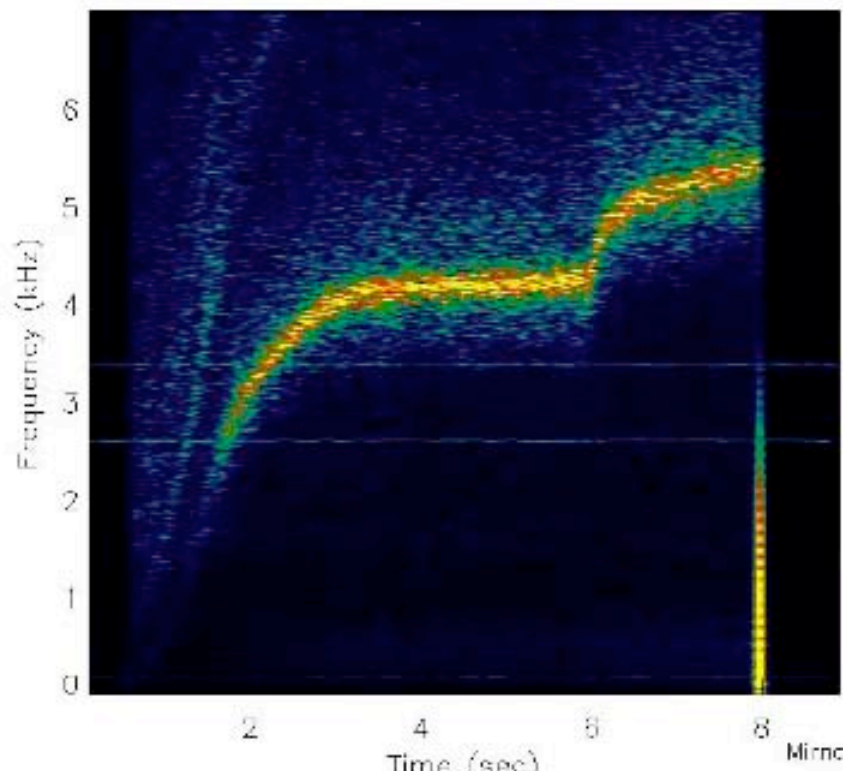
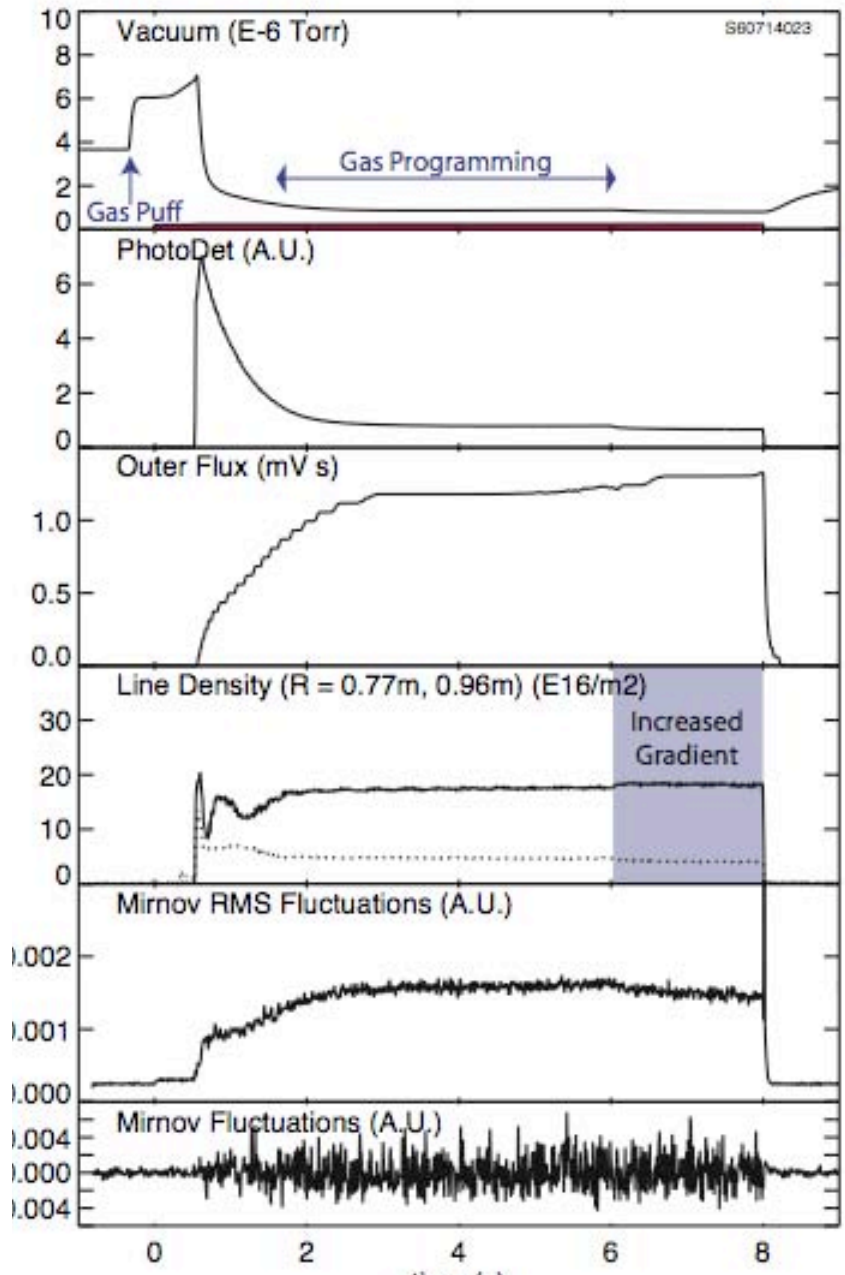


Real frequency is introduced for T_e/T_i

Quasi-coherent low frequency mode

- Under good vacuum conditions $p_0 < 10^{-6}$, quasi-coherent low frequency activity observed: $f < 10$ kHz
- Mode seen on Mirnov, edge probes, photodiodes, interferometer.
- Gas fueling can change frequency or stabilize mode
 - Cutoff fueling \Rightarrow mode frequency rises
 - Sufficient fueling \Rightarrow quasi-coherent mode disappears
 - ◆ Gas fueling tends to flatten the density gradient as seen in 60 GHz μ -wave interferometer array.
- Mirnov array indicates toroidal mode # $m=1$

Low Frequency Fluctuations Modified by Density Gradient



Mode appears to be $m=1$

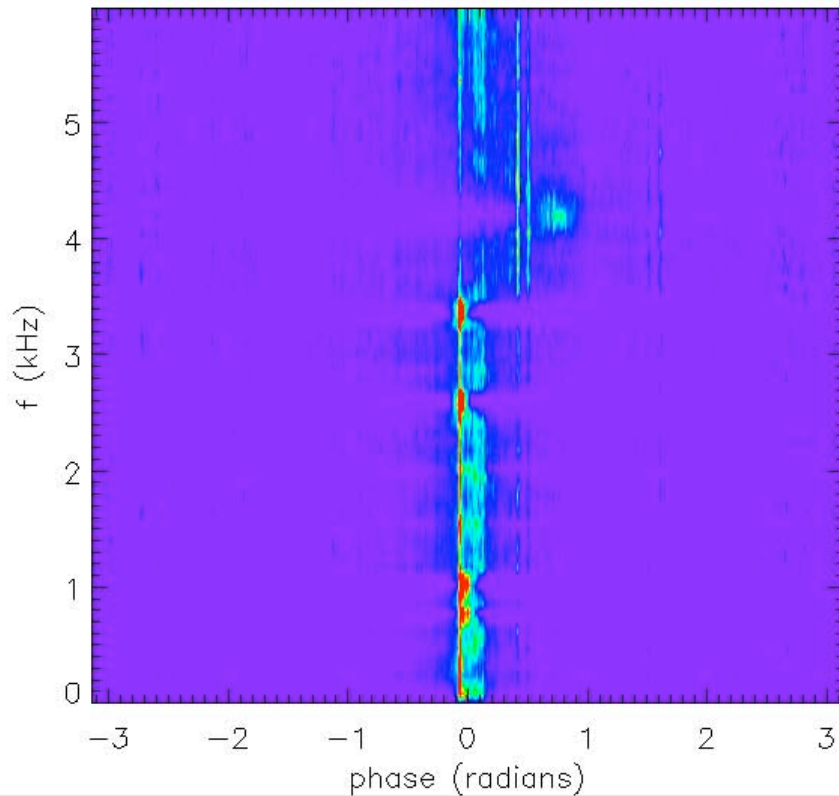
Use 8 Mirnov coils separated by 45 degrees

Ref: Beall, Kim, Powers, J App Phys 6 (82) 3933.

For $5 < t < 6$ s,

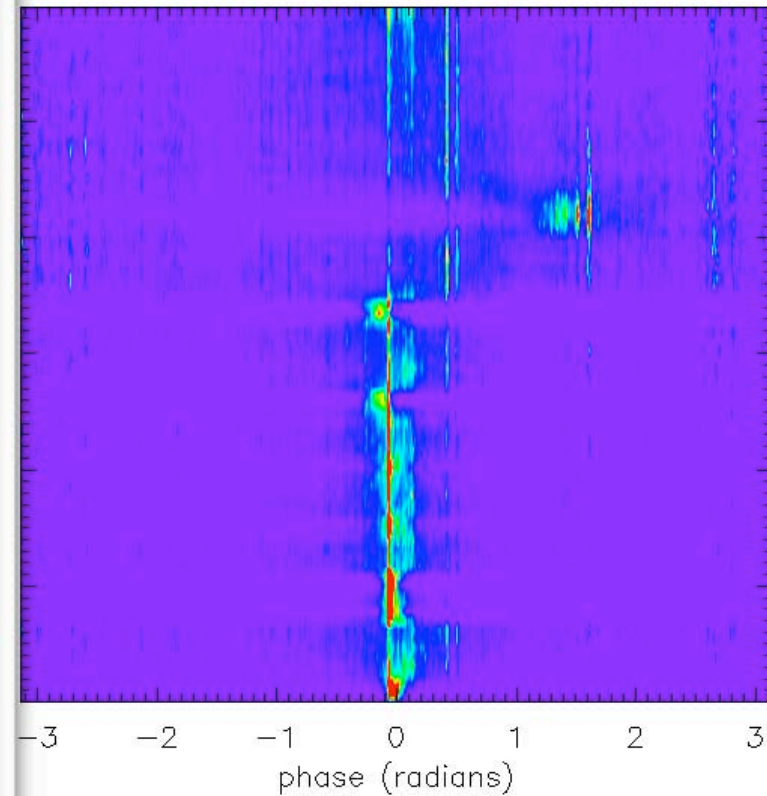
coil separation 45 deg

Mirnov coils, 7 with 6

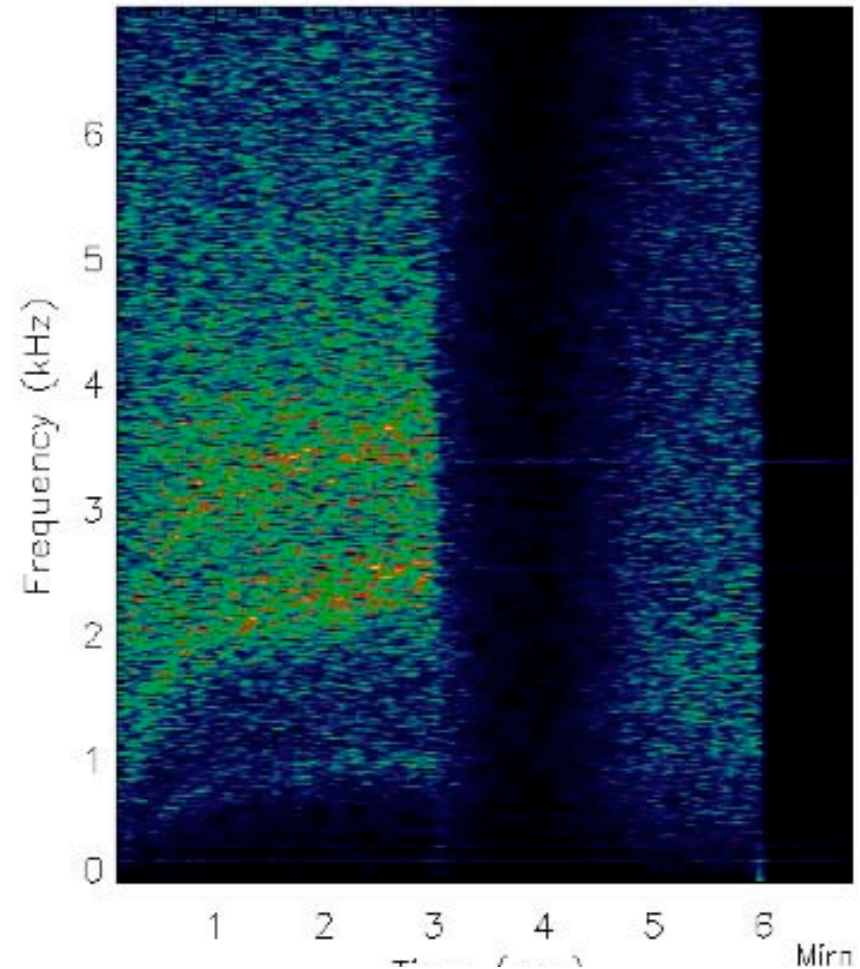
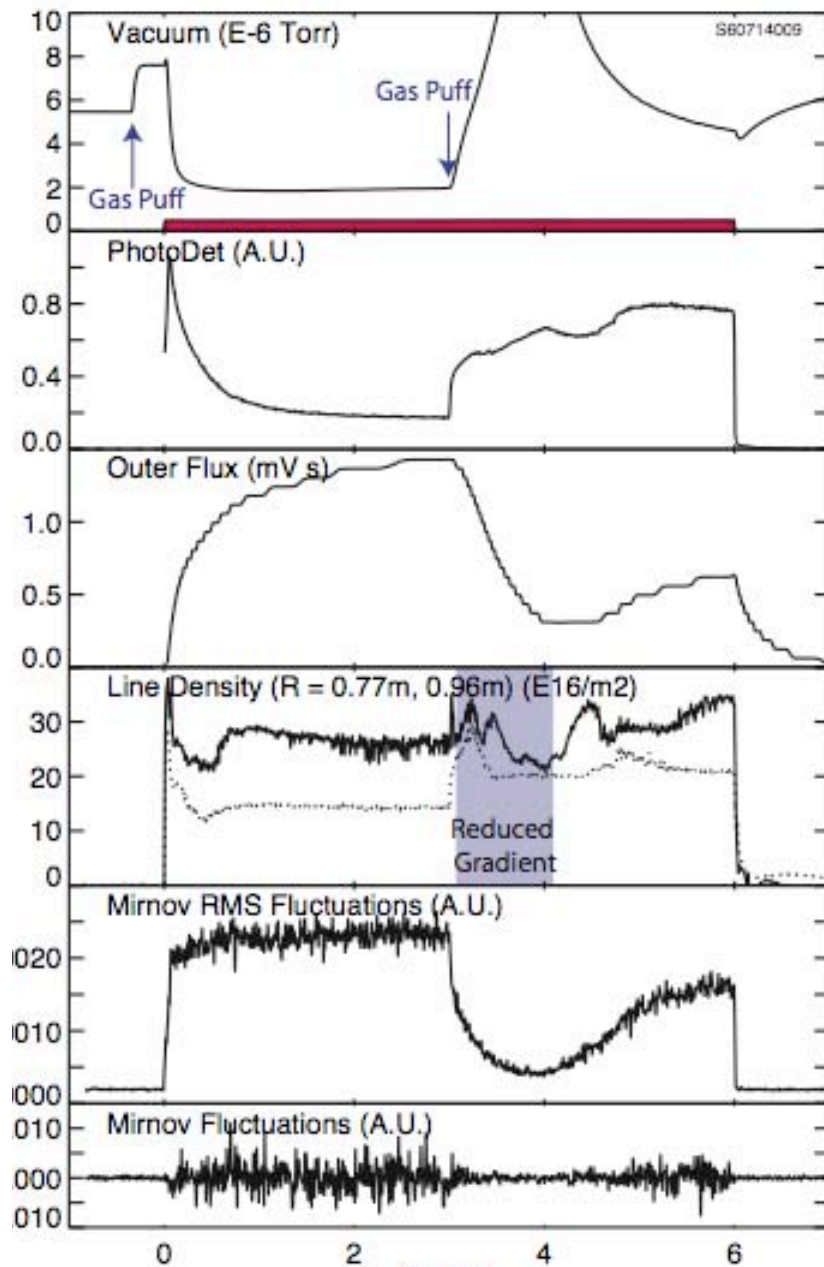


90 deg

Mirnov coils, 6 with 8



Fluctuations Suppressed with Flat Gradient

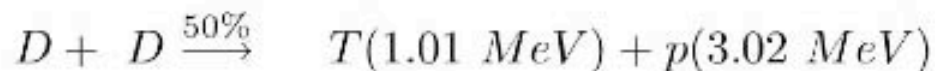
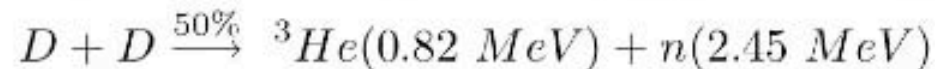
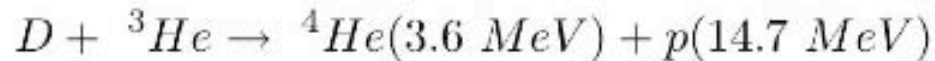
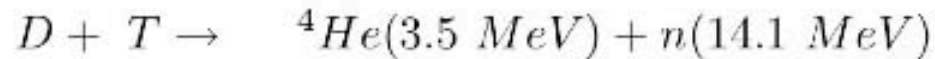


Requirements for “Ideal” fusion power source

- MHD does not destroy confinement (no disruptions)
- Intrinsically Steady State
- High β for economic field utilization
- High τ_E necessary for ignition
 - Ignition in small device
 - Advanced fuels (D-D, D-³He)
- Low τ_p for ash removal
- Low divertor heat load - want plasma outside of coils for flux expansion
- Circular, non-interlocking coils

Levitated dipole may fulfill these requirements if the physics and technology does not produce show-stopper.

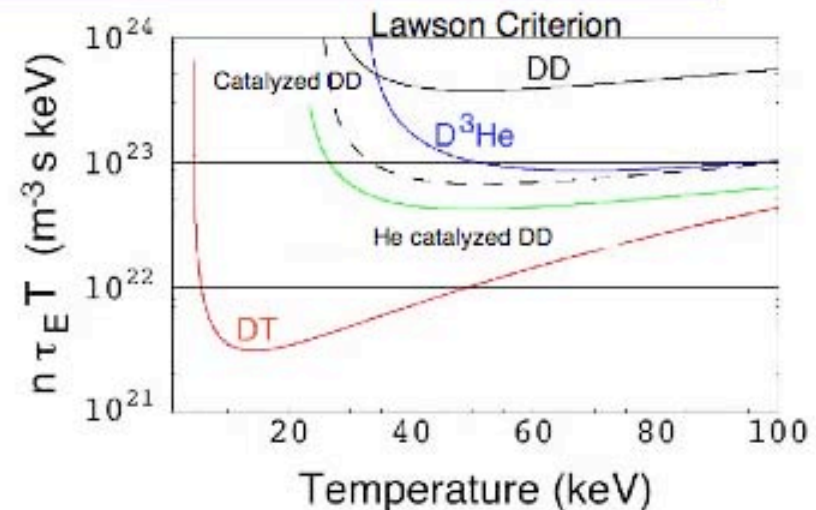
Fusion reactions of primary interest



- **D-T: Highest fusion x-section**
 - Must breed tritium
 - 14.1 MeV neutrons (a) Damage and activate structure
(b) Necessitate a massive shield
- **D-³He: Lower x-section, reduced neutron flux**
 - ³He source requires lunar mining
- **D-D: Smallest x-section - Ignition requires decoupling of particle and energy confinement [Ref: Nevins, JFE 17 (1998) 25.]**
 - Plentiful fuel source
 - Can eliminate energetic energetic neutrons if we can eliminate tritium
 - Fusion products mostly charged particles - **eliminate blanket and shield**
 - **high power/volume**

Helium Catalyzed D-D (self fueled D-³He cycle)

- Primary D-D reaction produces 3.65 MeV plus T & ³He.
- Permit the ³He to burn.
 - D-³He produces 18.3 MeV.
- Remove T and re inject the ³He decay product (T → ³He + e⁻).
 - Some T will fuse (4 to 6%) before removal, (during slowing down).
- This produces 22 MeV per DD fusion with 94% of power in charged particles (along with a 2.45 MeV neutron)
 - Surface heating → thin walled vessel with high power density
 - 2.45 MeV neutron produces little structural damage



Ref: Sawan et al, Fus Eng and Design **61-62** (2002), 561.

Kesner et al., Nuc Fus **44** (2004) 193.

Next Step: Levitation

- **Fast electron losses to supports eliminated**
 - ▶ Pitch angle scattering reduce anisotropy, not beta
 - ▶ Anisotropy driven modes relax plasma without losses
- **Bulk plasma confinement also improved**
 - ▶ Stable fast electron fraction with lower neutral gas fueling ?
- **Radial transport driven profiles**
 - ▶ Single peaked, broader (more stable) profiles
- ➔ **Expectation of improved stability and confinement**
 - ▶ Contrast with supported operation will further understanding of unstable/high- β regime bifurcation.

Conclusions and Future Plans

- LDX is novel in both physics and technology
 - Only superconducting experiment in US program
- LDX began operation on 2004: Observe 3 operating regimes
 - In high n_e regime $\beta \sim 20\%$, $T_{eh} \sim 50$ KeV.
 - Observe MHD events (HEI limits).
 - Multiple frequency ECRH provides profile control.
 - Can operate with magnetic separatrix
Shaping coil permits variation of flux expansion.
- Levitation experiments planned for late fall
 - Will eliminate pitch-angle scatter as loss mechanism
 - Expect substantial increase in plasma parameters
 - 10.5 GHz to be brought on line
 - Later 18 and 28 GHz